

# Math 107

Fall 2016

## Lecture 8

Translate only:

Twice the difference between 10 and Some number is equal to the Sum of Square of the number and -10.

$$2(10 - x) = x^2 + (-10)$$

$$2(10 - x) = x^2 - 10$$

What percent of 400 is 25?

$$\frac{P}{100} = \frac{\text{Part}}{\text{whole}} \quad \text{"whole comes after of"}$$

$$\frac{P}{100} = \frac{25}{400}$$

Cross-multiply

$$400P = 25(100)$$

6.25% of 400 is 25.

$$P = \frac{25(100)}{400} = \frac{25}{4} = 6.25$$

72 of 120 students had iPhone.

At this rate, how many students have iPhone if we have 4000 students?

$$\frac{72 \text{ iPhone}}{120 \text{ Students}} = \frac{x \text{ iPhone}}{4000 \text{ Students}}$$

$$\frac{72}{120} = \frac{x}{4000}$$

Cross-Multiply

$$120x = 72(4000)$$

$$x = \frac{72(4000)}{120}$$

$$x = 2400$$

2400 students have iPhone.

In a townhall meeting, There were 67 people.  
 The number of females was 1 fewer than  
3 times the number of males.

How many of each?

Females  $\rightarrow 3x - 1$

Males  $\rightarrow x$

17 Males  
 &  
 50 Females

Total = 67

Males + Females = 67

$$x + 3x - 1 = 67$$

$$4x - 1 = 67$$

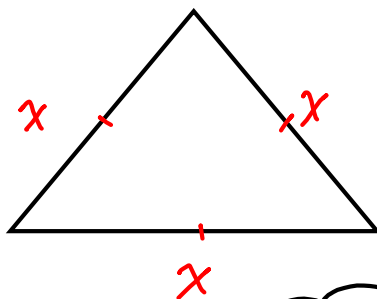
$$4x = 67 + 1$$

$$4x = 68$$

$$x = \frac{68}{4} \quad \boxed{x=17}$$

$$\frac{3(17)-1}{51-1}=50$$

A triangular billboard has a perimeter of 57 ft. All 3 sides are equal. Find how long each side is.



$$P = 57$$

$$a + b + c = 57$$

$$x + x + x = 57$$

$$3x = 57$$

$$x = \frac{57}{3} \quad x = 19$$

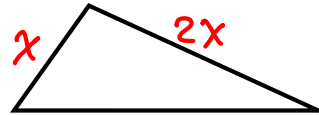
each side is 19 ft.

The perimeter of a triangular garden is 66 meters.

One side is twice another side.

The third side is 6 m shorter than 3 times the shorter side of first two sides.

Find all 3 sides.



Side 1  $\rightarrow x \rightarrow 12\text{ m}$

Side 2  $\rightarrow 2x \rightarrow 24\text{ m, and}$

Side 3  $\rightarrow 3x-6 \rightarrow 30\text{ m}$

$3x-6$

$P = 66$

$$a + b + c = 66$$

$$\downarrow \quad \downarrow \quad \downarrow$$

$$x + 2x + 3x - 6 = 66$$

$$6x - 6 = 66$$

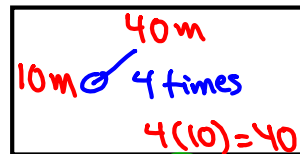
$$6x = 66 + 6$$

$$6x = 72$$

$$x = 12 \rightarrow x = \frac{72}{6}$$

The length of a rectangular room is 4 times its width.

The perimeter is 100 m.



$$W = x$$

1) find its dimensions.

10m by 40m

$$P = 100$$

$$L = 4x$$

$$2L + 2W = 100$$

$$2(4x) + 2(x) = 100$$

$$8x + 2x = 100$$

$$10x = 100$$

$$x = \frac{100}{10}$$

$$x = 10$$

2) find its area.

3) find cost for carpet if it is \$4/Sqr. meter.

$$A = LW$$

$$= 40(10)$$

$$A = 400 \text{ m}^2$$

$$\text{Cost} = 4(400)$$

$$\boxed{\$1600}$$

The width of a rectangular field is 10 ft shorter than its length.

The perimeter is 180 ft.

find its area.

$$P = 180$$

$$2L + 2W = 180$$

$$2x + 2(x - 10) = 180$$

$$\underline{2x + 2x - 20 = 180}$$

$$4x - 20 = 180$$

$$4x = 180 + 20$$

40 ft  
50 ft

$$W = x - 10$$

$$L = x$$

$$4x = 200$$

$$x = \frac{200}{4}$$

$$x = 50$$

$$A = LW$$

$$= 50(40)$$

$$= 2000 \text{ ft}^2$$

A rectangle has perimeter of 306 in.

The length is 1 in. longer than 3 times its width.

find the measure of its length.

A) 38

B) 38 in.

C) 115

D) 115 in.

$$\text{Length} \rightarrow 3x + 1$$

$$\text{Width} \rightarrow x$$

$$3(38) + 1$$

$$= 114 + 1$$

$$= 115$$

$$P = 306$$

$$2L + 2W = 306$$

$$2(3x + 1) + 2x = 306$$

$$6x + 2 + 2x = 306$$

$$8x + 2 = 306$$

$$8x = 306 - 2$$

$$8x = 304$$

$$x = \frac{304}{8}$$

$$x = 38$$